

# Errata

## Transverse Shear Deformation in Orthotropic Cylindrical Pressure Vessels Using a Higher-Order Shear Theory

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The following errors were inadvertently introduced during production of the paper:

### Page 1441

The fifth sentence of the first paragraph should have Refs. 1 and 3, not Ref. 13.

### Page 1442

Equation (2) should appear as follows; changes are indicated in bold face:

$$\begin{Bmatrix} \sigma_1 \\ \sigma_2 \\ \sigma_6 \\ \sigma_4 \\ \sigma_5 \end{Bmatrix} = \begin{bmatrix} Q_{11} & Q_{12} & 0 & 0 & 0 \\ Q_{12} & Q_{22} & 0 & 0 & 0 \\ 0 & 0 & Q_{66} & 0 & 0 \\ 0 & 0 & 0 & Q_{44} & 0 \\ 0 & 0 & 0 & 0 & Q_{55} \end{bmatrix} \begin{Bmatrix} \epsilon_1 \\ \epsilon_2 \\ \epsilon_6 \\ \epsilon_4 \\ \epsilon_5 \end{Bmatrix} \quad (2)$$

Equation (3) should be

$$\begin{aligned} Q_{11} &= E_1/\Delta, & Q_{12} &= \nu_{12}E_2/\Delta, & Q_{22} &= E_2/\Delta \\ Q_{66} &= G_{12}, & Q_{44} &= G_{23}, & Q_{55} &= G_{13} \end{aligned} \quad (3)$$

where  $Q_{ij} = C_{ij} - [(C_{13}C_{j3})/C_{33}]$ , in which  $C_{ij}$  are functions of engineering constants,  $\nu_{ij}$ ,  $E_i$ , and  $G_{ij}$ , and  $C_{22} = C_{33}$ ,  $C_{12} = C_{13}$ .

The second sentence after Eq. (3) should read as follows:

In general, the fibers of the  $k$ th individual layer or ply are oriented at an angle  $\Phi$ , as shown in Fig. 2 for a cylindrical shell with coordinates  $\xi_1 = x$ ,  $\xi_2 = s$ , and  $\zeta$ .

The two sentences after Eq. (4b) should read as follows:

where  $\bar{Q}_{ij}$  ( $i, j = 1, 2, 6$ ) and  $\bar{Q}_{mn}$  ( $m, n = 4, 5$ ) are elements of symmetric arrays of transformed stiffness for the  $k$ th ply, and

$\sigma_k$  and  $\epsilon_k$  are measured with respect to shell coordinates  $\xi_\alpha$  ( $\alpha = 1, 2$ ) and  $\zeta$ .

Therefore, from Eq. (2) or (4), if the transverse stresses  $\sigma_4$  and  $\sigma_5$  vanish on the top and bottom surfaces of the shell, as stated in assumption 4, it is also true that the transverse shear strains vanish on those surfaces.

Equation (5a) should be

$$u_1(\xi_1, \xi_2, \zeta) = u(1 - \zeta/R_1) + \zeta\psi_1 + \zeta^2\phi_1 + \zeta^3\gamma_1 + \zeta^4\theta_1 \quad (5a)$$

In Eq. (7c),  $(h^2/8R_2^2)$  should be underlined as printed here.

$$[1 - (h^2/8R_2^2)]\gamma_2 \approx \gamma_2 = (-4/3h^2)[\psi_2 + (w_{,2}/\alpha_2)] \quad (7c)$$

### Page 1443

The fourth sentence in the first paragraph should read as follows, with changes in bold face:

A similar exercise is applied to  $\epsilon_5$ .

The second and third sentences under Strain Displacement Relations should read:

After scale-factor expressions are approximated by truncated binomial series, the in-plane strains can be represented as in Eq. (9), where the terms extend to  $\zeta^7$ . The  $\epsilon_i^0$  and  $\kappa_{ip}$  terms represent algebraically complicated nonlinear terms in displacement and are functions of the surface parameters  $\xi_1$  and  $\xi_2$ .

The first line of Eq. (14) should appear as printed here:

$$U_1 = \frac{1}{2} \int_{\Omega} (u_1 + u_2 + u_3) d\Omega \quad (14)$$

There should be spaces between  $u$  and  $u_{,1}$ ,  $v$  and  $v_{,1}$ , and  $w$  and  $w_{,1}$  in Eq. (17), as follows:

$$\begin{aligned} d^T = \{ & u u_{,1} u_{,2} v v_{,1} v_{,2} w w_{,1} w_{,2} w_{,11} w_{,22} w_{,12} \psi_1 \psi_{1,1} \psi_{1,2} \\ & \psi_2 \psi_{2,1} \psi_{2,2} \} \end{aligned} \quad (17)$$

Change the term  $[-69/0/60]_s$  in the fifth line under Fig. 6 so that it reads:

$$[-60/0/60]_s$$

Equation (A3) should be as it is printed here, with changes in bold face:

$$\kappa_{11} = \psi_{1,1} - v_{,1}^2 c^2 + \psi_{1,1} u_{,1} + \psi_{2,1} v_{,1} \quad (A3)$$

The last term in Eq. (A8),  $+\psi_{2,1}^2$ , should be deleted.

The second addition sign in the second line of Eq. (A13) should be deleted so that the line appears as follows:

$$\dots + v\psi_2 c^3 - 2c^2(\psi_{2,2}w - \psi_2 w_{,2}) + \psi_{2,2}w_{,2}c \quad (A13)$$

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An addition sign should appear in the last line of Eq. (A15) as printed here in bold face:

$$\dots + w_{,2}\psi_2 + \psi_{1,2}k(w_{,12} + \psi_{1,2}) + \psi_2kc^2(w_{,2} + \psi_2) \quad (\text{A15})$$

The first line of Eq. (A16) should be:

$$\kappa_{25} = 2kc[\psi_{2,2}(w_{,22} + \psi_{2,2}) + \psi_{1,2}(w_{,12} + \psi_{1,2})$$

The second line of Eq. (A21) should begin with + c. Also, delete the second  $w_{,1} w_{,2}$  term. The corrected line should read:

$$\dots + c(u_{,1}u_{,2} - v_{,1}v_{,2} + w_{,1}w_{,2} - w\psi_{2,1} + w_{,1}\psi_2)$$

Replace 1 with 2 in the first term of the first line of Eq. (A23), and the second term of the fourth line of Eq. (A23) should be

$\psi_{2,1}\psi_{2,2}$  as printed here:

$$\begin{aligned} \kappa_{63} = & 2kw_{,12} + k\psi_{1,2} + k\psi_{2,1} + ku_{,2}(w_{,11} + \psi_{1,1}) \\ & + kcw_{,1}(w_{,2} + \psi_2) - ku_{,1}(w_{,12} + \psi_{1,2}) \\ & + kv_{,1}(w_{,22} + \psi_{2,2}) - kcw(w_{,12} + \psi_{2,1}) \\ & + c(\psi_{1,1}\psi_{1,2} + \psi_{2,1}\psi_{2,2}) + kv_{,2}(w_{,12} + \psi_{2,1}) \end{aligned} \quad (\text{A23})$$

Replace  $w_{,1} w_{,2}$  with  $w\psi_{2,1} - w_{,1} w_{,2}$  at the end of the third line of Eq. (A24) so that it reads

$$\dots + \psi_{2,2}(w_{,12} + \psi_{2,1}) - kc^2(w w_{,12} + w\psi_{2,1} - w_{,1}w_{,2}) \quad (\text{A24})$$

The last term of Eq. (A33) should be  $\kappa_{j7}\kappa_{i7}T_{ij}$  as printed here:

$$\dots + (2\kappa_{j5}\kappa_{i7} + \kappa_{j6}\kappa_{i6})R_{ij} + 2\kappa_{j6}\kappa_{i7}S_{ij} + \kappa_{j7}\kappa_{i7}T_{ij} \quad (\text{A33})$$

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